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Since it takes the policeman $\frac{1}{2}$ mile, it will take him 6 minutes to overtake the auto and end the race.

In the statement of this problem, the semi-colon should be omitted after the word "started." With this omission the problem was solved as above by J. W. Clawson, V. M. Spunar, J. H. Meyer. R. D. Carmichael, A. H. Holmes, B. Kramer; J. Scheffer, J. K. Ellwood, and P. S. Berg, interpreting the problem as printed, agree in the answer being 2 hours, 36 minutes.

GEOMETRY.

336. Proposed by F. H. HODGE, The University of Chicago.

A man owning a rectangular field $b=300$ feet by $a=600$ feet, wishes to lay out driveways of equal width having the diagonals of the field as center lines and such that the area of the driveways shall be $n/m=$ one-half, of the area of the field. Determine the width of the driveways.

Solution by J. SCHEFFER, A. M., Hagerstown, Md.; NELLIE WOOD, Senior Class, Drury College, Springfield, Mo.; and A. H. HOLMES, Brunswick, Me.

Put $AE=x$; then $AG=\frac{bx}{a}$; $\triangle EFK=\triangle GHL=\frac{b}{a} \cdot \frac{(a-2x)^2}{4}$.

\therefore space occupied by driveways $= ab - \frac{b}{a} (a-2x)^2$.

$\therefore ab - \frac{b}{a} (a-2x)^2 = \frac{n}{m} ab$; whence

$$x = \frac{1}{2}a \left(1 - \sqrt{1 - \frac{n}{m}} \right).$$

\therefore breadth of driveway $= \frac{ab}{\sqrt{(a^2+b^2)}} \left(1 - \sqrt{1 - \frac{n}{m}} \right)$.

For $a=600$, $b=300$, $n:m=1:2$, we find breadth $= 60(2\sqrt{5}-\sqrt{10})=78.572$ feet.

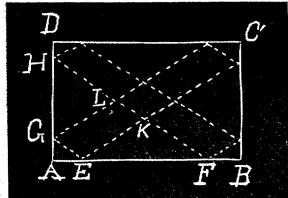
Also solved by B. Kramer, V. M. Spunar, G. I. Hopkins, J. H. Meyer, G. B. M. Zerr, and A. H. Bell.

337. Proposed by T. N. HILDEBRANT, The University of Chicago.

Required the locus of the vertices of the parabolae having a given focus and passing through a given point.

Solution by the PROPOSER.

Let O be the given focus and P the given point. From the properties of the parabola we see that the directrices of the parabolae passing through P will be the tangents to the circle of radius OP and center P . Hence the vertices will be the mid-points D of the perpendiculars from O to the tangents. From elementary geometry we have the triangles OCB and OAB equal, and therefore $OC=OA=x_1$, the abscissa of B the point of tangency, if we suppose O the origin of our system of coordinates. Hence $OD=\frac{1}{2}x_1$. Denote by α the angle POC . Then we also have $EPB=\alpha$. Evidently



$$x_1 = OP + PA = a + a \cos \alpha = a(1 + \cos \alpha); \text{ i. e., } OD = \frac{1}{2}x_1 = \frac{a}{2}(1 + \cos \alpha),$$

which gives as the polar equation of the locus referred to O as origin and OP as initial line,

$$\rho = \frac{a}{2}(1 + \cos \alpha),$$

a cardioid, with cusp at O passing through P and having OP as line of symmetry.

Also solved by J. Scheffer, A. H. Holmes, V. M. Spunar, G. B. M. Zerr, and J. W. Clawson.

CALCULUS.

264. Proposed by W. J. GREENSTREET, M. A., Stroud, England.

The join of the center of curvature of a curve to the origin is at α to the initial line. Prove that with the usual notation:

$$\frac{d \alpha}{d \psi} \left[\left(\frac{dp}{d \psi} \right)^2 + \left(\frac{d^2 p}{d \psi^2} \right)^2 \right] = \frac{dp}{d \psi} \cdot \frac{d \rho}{d \psi}.$$

Solution by V. M. SPUNAR, M. and E. E., East Pittsburg, Pa.

Denote the coordinates of the center of curvature by ξ, η . Then $\xi = x - \rho \sin \phi, \eta = y + \rho \cos \phi$, ρ being the radius of curvature and ϕ the angle formed by the tangent and positive x -axis.

$$\therefore \tan \alpha = \eta / \xi, \text{ and } d \alpha = \frac{\xi d \eta - \eta d \xi}{\xi^2 + \eta^2}.$$

Likewise, $\tan \phi = r \frac{d \theta}{d r}$, and $d \phi = \left[d \theta + r \left(\frac{d^2 \theta}{d r^2} \right) \right] \div \sec^2 \phi$, where ϕ = angle included by the tangent at (r, θ) , and the radius vector to the point (r, θ) .

Substituting the proper values of $\xi, \eta, d \xi, d \eta$ in $d \alpha$, expressed in polar coordinates, and we have the first product $d \alpha / d \phi$.

Also, on remembering that $\left\{ \begin{array}{l} p = r \sin \phi \\ \phi = \theta + \psi \end{array} \right\}$, differentiate it twice, square every differential quotient as indicated by the proposition, add the like terms, reduce, and we have, readily,

$$\frac{d \alpha}{d \psi} \left[\left(\frac{dp}{d \psi} \right)^2 + \left(\frac{d^2 p}{d \psi^2} \right)^2 \right] = \frac{dp}{d \psi} \cdot \frac{d \rho}{d \psi}.$$

265. Proposed by V. M. SPUNAR, M. and E. E., East Pittsburg, Pa.

Find two curves which possess the property that the tangents TP and TQ to the inner one always makes equal angles with the tangent TT' to the outer.